

FOURIER-TRANSZFORMÁCIÓ alaptulajdonságai

$$\mathcal{F}(f(x) + g(x); s) = \mathcal{F}(f(x); s) + \mathcal{F}(g(x); s)$$

$$\mathcal{F}(c \cdot f(x); s) = c \cdot \mathcal{F}(f(x); s) \quad (c \in \mathbb{C})$$

$$\mathcal{F}(f(ax); s) = \frac{1}{a} \mathcal{F}\left(f(x); \frac{s}{a}\right) \quad (a > 0)$$

$$\mathcal{F}(f(-x); s) = \mathcal{F}(f(x); -s)$$

$$\mathcal{F}(f(x - x_0); s) = e^{-isx_0} \cdot \mathcal{F}(f(x); s)$$

$$\mathcal{F}(e^{i\omega_0 x} \cdot f(x); s) = \mathcal{F}(f(x); s - \omega_0)$$

$$\mathcal{F}(x \cdot f(x); s) = i \cdot \frac{d}{ds} \mathcal{F}(f(x); s)$$

$$\mathcal{F}(f'(x); s) = is \cdot \mathcal{F}(f(x); s)$$

Alap-Fourier-transzformáltak:

$$1. \quad \mathcal{F}(e^{-|x|}; s) = \sqrt{\frac{2}{\pi}} \cdot \frac{1}{1 + s^2}$$

$$2. \quad \mathcal{F}(e^{-x^2/2}; s) = e^{-s^2/2}$$

$$3. \quad f(x) = \begin{cases} 1 & \text{ha } -1 < x < 1 \\ 0 & \text{ha } |x| > 1 \end{cases} \quad \text{esetén}$$

$$\mathcal{F}(f(x); s) = \sqrt{\frac{2}{\pi}} \cdot \frac{\sin s}{s}.$$